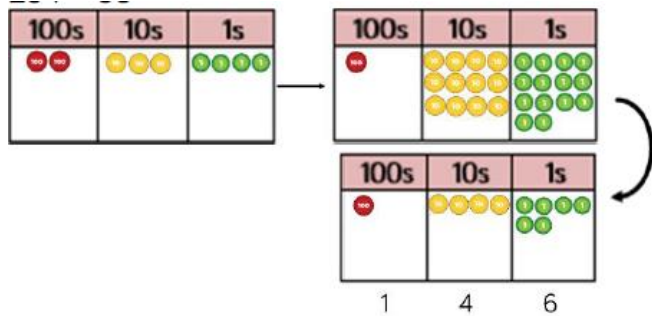
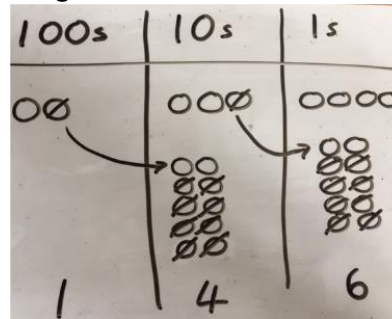


Column method using place value counters or Diene's. HTO – TO.

$$234 - 88$$



Represent the place value counters pictorially; remembering to show what has been exchanged.

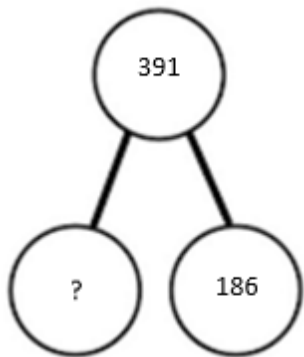


Formal column method. Children must understand what has happened when they have crossed out digits. This should be applied to larger numbers once secure.

$$\begin{array}{r} \overset{2}{2} \overset{1}{3} 4 \\ - 88 \\ \hline 6 \end{array}$$

Fluency variation, different ways to ask children to solve 391 – 186:

391	
186	?



Raj spent £391, Timmy spent £186.
How much more did Raj spend?

Calculate the difference between 391 and 186.

$$\square = 391 - 186$$

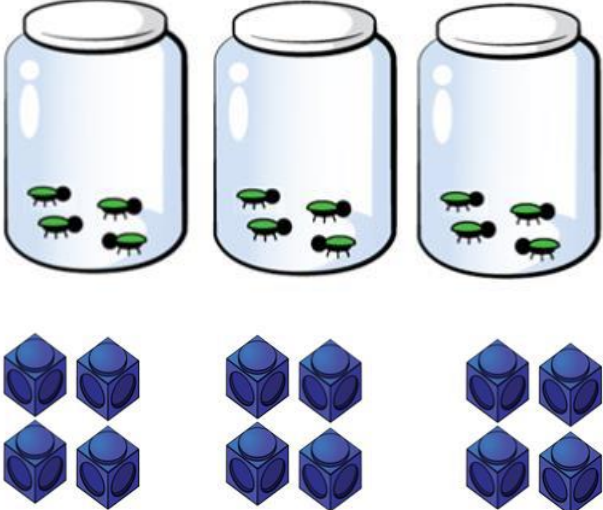
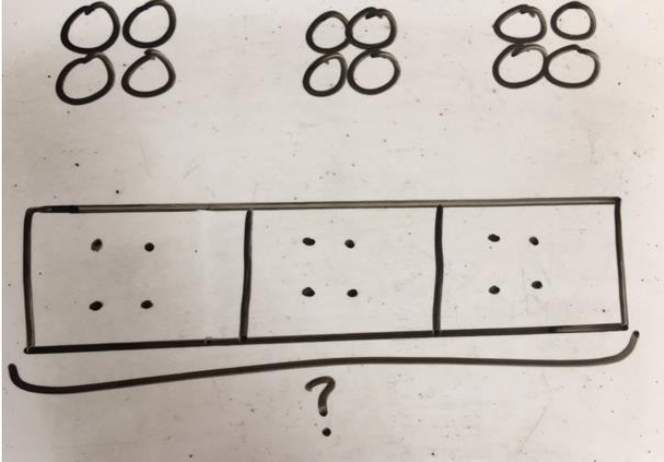
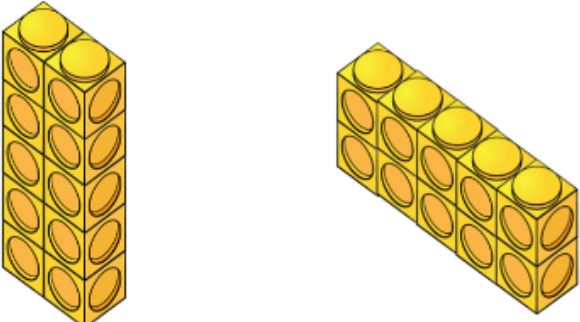
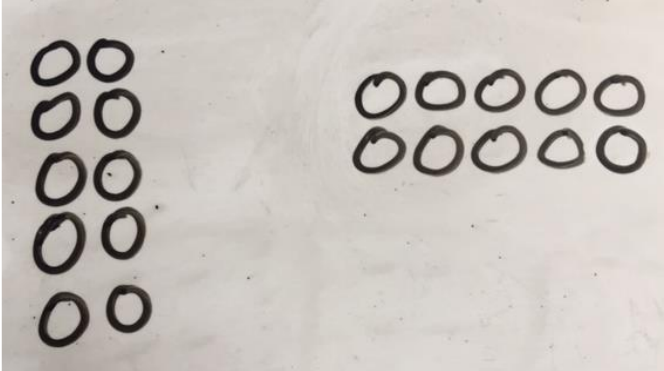
$$\begin{array}{r} 391 \\ - 186 \\ \hline \end{array}$$

What is 186 less than 391?

Missing digit calculations:

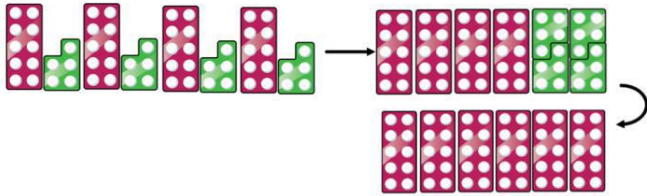
$$\begin{array}{r} 39\square \\ - \square\square 6 \\ \hline \square 0 5 \end{array}$$

Multiplication

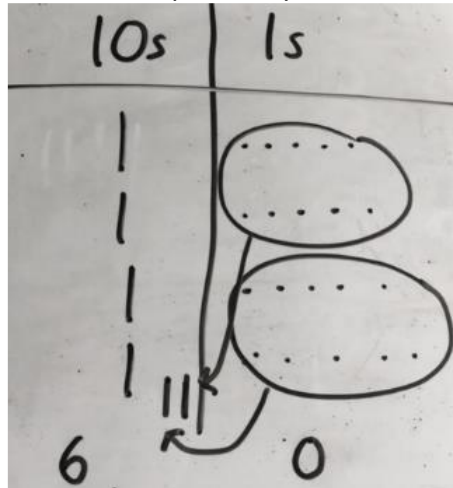
Concrete	Pictorial	Abstract
<p>Repeated grouping/repeated addition</p> <p>3×4 $4 + 4 + 4$</p> <p>There are 3 equal groups, with 4 in each group.</p> 	<p>Children to represent the practical resources in a picture and use a bar model.</p> 	<p>Abstract</p> <p>$3 \times 4 = 12$</p> <p>$4 + 4 + 4 = 12$</p>
<p>Use arrays to illustrate commutativity counters and other objects can also be used.</p> <p>$2 \times 5 = 5 \times 2$</p>  <p>2 lots of 5 5 lots of 2</p>	<p>Children to represent the arrays pictorially.</p> 	<p>Children to be able to use an array to write a range of calculations e.g.</p> <p>$2 \times 5 = 10$ $5 \times 2 = 10$ $2 + 2 + 2 + 2 + 2 = 10$ $5 + 5 = 10$</p>

Partition to multiply using Numicon, base 10 or Cuisenaire rods.

4×15



Children to represent the concrete manipulatives pictorially.



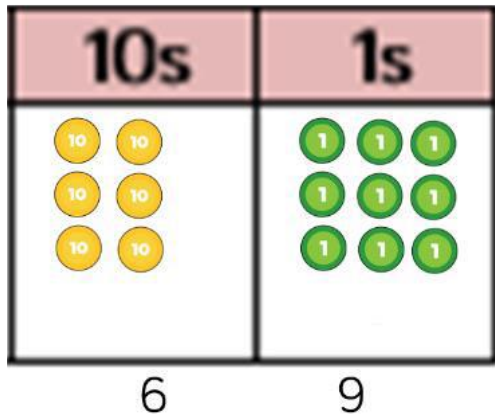
Children to be encouraged to show the steps they have taken.

$$\begin{array}{r} 4 \times 15 \\ \swarrow \searrow \\ 10 \quad 5 \end{array}$$

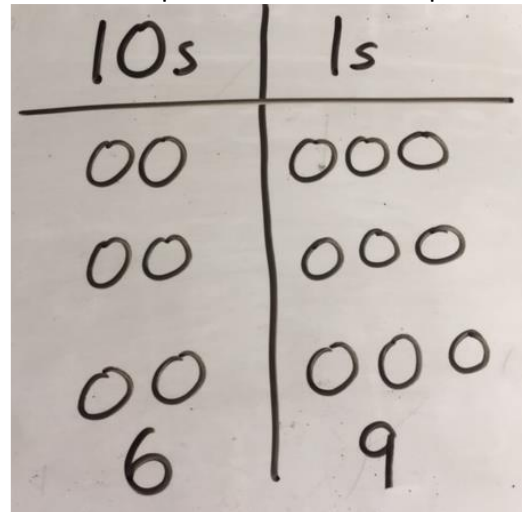
$$\begin{array}{l} 10 \times 4 = 40 \\ 5 \times 4 = 20 \\ 40 + 20 = 60 \end{array}$$

Formal column method with place value counters (base 10 can also be used.)

3×23



Children to represent the counters pictorially.



Children to record what it is they are doing to show understanding.

$$\begin{array}{r} 3 \times 23 \\ \swarrow \searrow \\ 20 \quad 3 \end{array} \quad \begin{array}{l} 3 \times 20 = 60 \\ 3 \times 3 = 9 \\ 60 + 9 = 69 \end{array}$$

$$\begin{array}{r} 23 \\ \times 3 \\ \hline 69 \end{array}$$

Children should partition the question in order to solve it.

6×23

$6 \times 20 = 120$

$6 \times 3 = 18$

$6 \times 23 = 138$

Formal written method

$6 \times 23 =$

$$\begin{array}{r} 23 \\ \times 6 \\ \hline 138 \\ \hline 11 \end{array}$$

When children start to multiply $3d \times 3d$ and $4d \times 2d$ etc., they should be confident with the abstract:

To get 744 children have solved 6×124 .

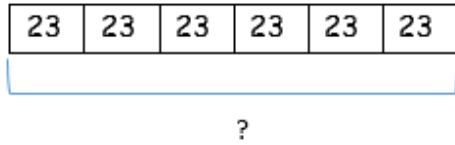
To get 2480 they have solved 20×124 .

$$\begin{array}{r} 124 \\ \times 26 \\ \hline 744 \\ 480 \\ \hline 3224 \\ \hline 11 \end{array}$$

Answer: 3224

Fluency variation, different ways to ask children to solve 6×23 :

Why is $6 \times 23 = 23 \times 6$?



Mai had to swim 23 lengths, 6 times a week.

How many lengths did she swim in one week?

With the counters, prove that $6 \times 23 = 138$

Find the product of 6 and 23

$6 \times 23 =$

$\square = 6 \times 23$

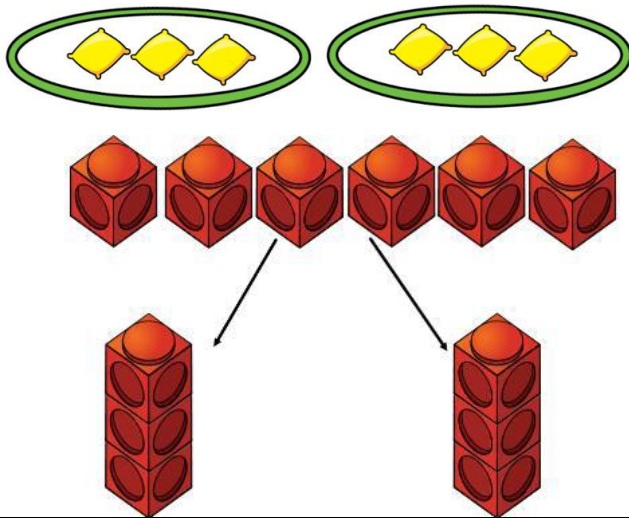
$$\begin{array}{r} 6 \quad 23 \\ \times 23 \quad \times 6 \\ \hline \end{array}$$

Division

Concrete

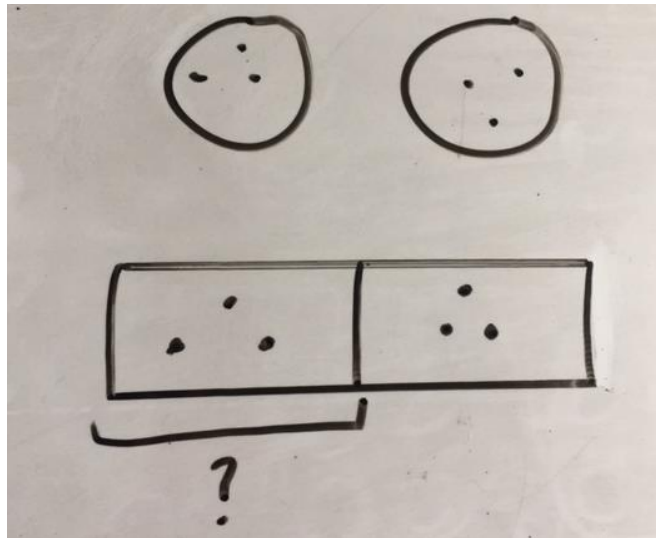
Sharing using a range of objects.

$6 \div 2$



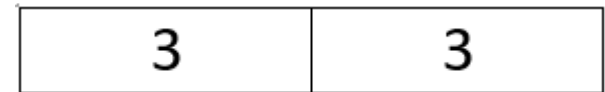
Pictorial

Represent the sharing pictorially.



Abstract

$6 \div 2 = 3$



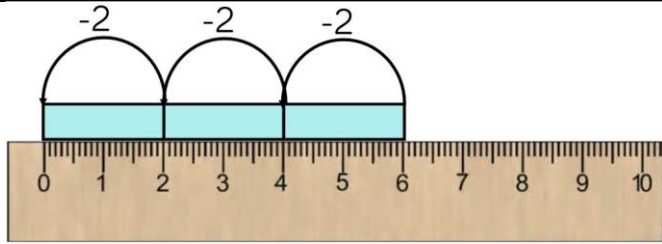
Children should also be encouraged to use their 2 times tables facts to share into 2 groups.

Repeated subtraction using Cuisenaire rods above a ruler.

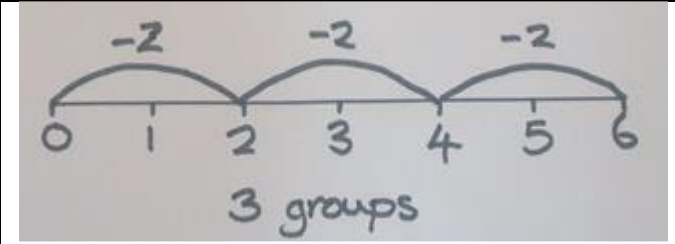
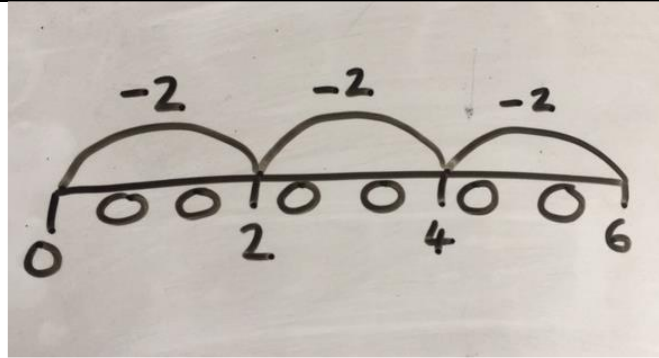
Children to represent repeated subtraction pictorially.

Abstract number line to represent the equal groups that have been subtracted.

$6 \div 2$

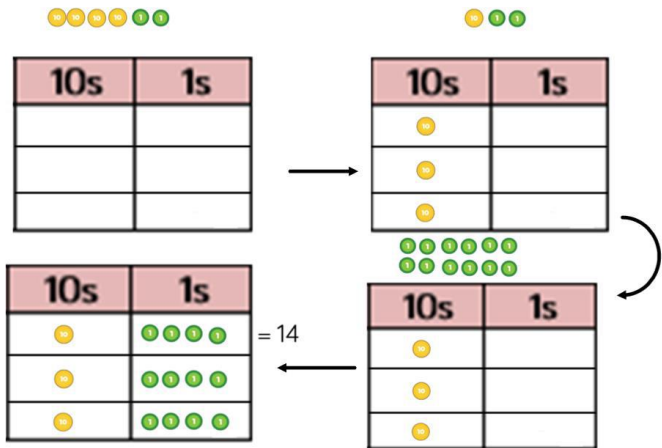


3 groups of 2

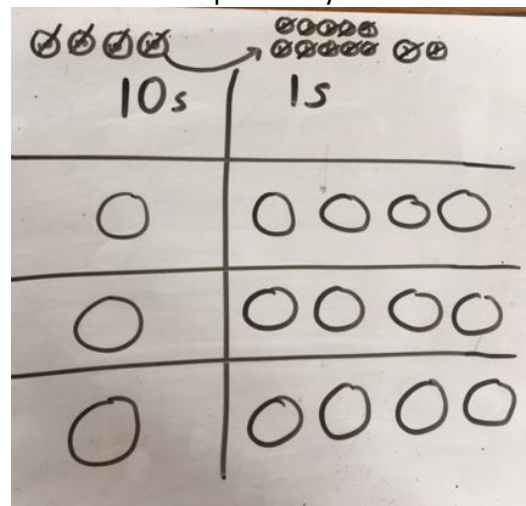


Sharing using place value counters.

$$42 \div 3 = 14$$



Children to represent the place value counters pictorially.



Children to be able to make sense of the place value counters and write calculations to show the process.

$$42 \div 3$$

$$42 = 30 + 12$$

$$30 \div 3 = 10$$

$$12 \div 3 = 4$$

$$10 + 4 = 14$$

Use of the 'bus stop method' to show short division.

$$5 \overline{) 123615}$$

Additionally, children should be shown how remainders can be turned into decimals at the end.

$$4 \overline{) 135.5}$$

$$4 \overline{) 5142.20}$$

Long Division

1) exchange two thousands for 20 hundreds, so we now have 25 hundreds.

$$12 \overline{) 2544}$$

2) How many groups of 12 can I make with 25 hundreds? The 24 shows the hundreds we have grouped. The one is how many hundreds we have left.

$$12 \overline{) 2544}$$

$$\underline{24}$$

$$14$$

$$\underline{12}$$

$$2$$

3) Exchange the one hundred for 10 tens. How many groups of 12 can I make with 14 tens? The 14 shows how many tens I have, the 12 is how many I grouped and the 2 is how many tens I have left.

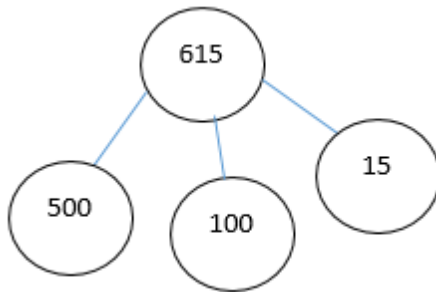
12

$$\begin{array}{r}
 0212 \\
 \overline{)2544} \\
 \underline{24} \\
 14 \\
 \underline{12} \\
 24 \\
 \underline{24} \\
 0
 \end{array}$$

4) Exchange the 2 tens for 20 ones. The 24 is how many ones I have grouped and the 0 is what I have left.

Fluency variation, different ways to ask children to solve $615 \div 5$

Using the part whole model below, how can you divide 615 by 5 without using short division?



I have £615 and share it equally between 5 bank accounts. How much will be in each account?

615 pupils need to be put into 5 groups. How many will be in each group?

$$5 \overline{)615}$$

$$615 \div 5 =$$

$$\square = 615 \div 5$$